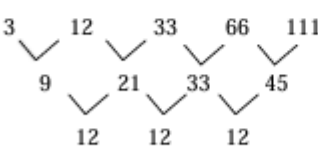


REVISION MARKING GUIDELINE 2025

QUESTION 1/VRAAG 1

1.1.1	$x^2 - 3x - 10 = 0$ $(x + 2)(x - 5) = 0$ $x = -2$ or $x = 5$	✓ factors ✓ $x = -2$ ✓ $x = 5$ (3)
1.1.2	$3x^2 + 6x + 1 = 0$ $x = \frac{-(6) \pm \sqrt{(6)^2 - 4(3)(1)}}{2(3)}$ $x = -1,82$ or $x = -0,18$	✓ correct substitution into the formula ✓ $x = -1,82$ ✓ $x = -0,18$ (3)
1.1.3	$2^{x+4} + 2^x = 8704$ $2^x(16 + 1) = 8704$ $2^x = 512 = 2^9$ OR $x = \log_2 512$ $x = 9$ = 9	✓ common factor ✓ simplification ✓ answer (3)
1.1.4	$(x - 8)(x + 2) \leq 0$ CV: $x = 8$ or $x = -2$ $\therefore -2 \leq x \leq 8$	✓ critical values ✓✓ $-2 \leq x \leq 8$ (3)
1.1.5	$x + 3\sqrt{x+2} = 2$ $3\sqrt{x+2} = 2 - x$ $9(x+2) = 4 - 4x + x^2$ $x^2 - 13x - 14 = 0$ $(x - 14)(x + 1) = 0$ $x \neq 14$ or $x = -1$	✓ isolating the surd ✓ squaring both sides ✓ standard form ✓ answer with selection (4)

QUESTION 2/VRAAG 2

2.1.1	$7 + 12 + 17 + \dots$ $T_n = a + (n-1)d$ $T_{91} = 7 + (91-1)(5)$ $T_{91} = 457$ OR/OF $d = 5$ $T_n = 5n + 2$ $T_{91} = 5(91) + 2$ $T_{91} = 457$	$\checkmark d = 5$ $\checkmark$ substitution into correct formula $\checkmark$ answer (3) OR/OF $\checkmark d = 5$ $\checkmark$ substitution $n = 91$ $\checkmark$ answer (3)
2.1.2	$S_n = \frac{n}{2}[2a + (n-1)d]$ $S_{91} = \frac{91}{2}[2 \times 7 + (91-1)(5)]$ $S_0 = 21\ 112$ OR/OF $S_n = \frac{n}{2}(a + l)$ $S_{91} = \frac{91}{2}(7 + 457)$ $S_{91} = 21\ 112$	$\checkmark$ substitution into correct formula $\checkmark$ answer (2) OR/OF $\checkmark$ substitution into correct formula $\checkmark$ answer (2)
2.1.3	$T_n = 7 + (n-1)(5)$ $5n + 2 = 517$ $5n = 515$ $n = 103$	$\checkmark$ substitution into correct formula $\checkmark$ equate $\checkmark$ answer (3)
2.2.1	$T_1 = 3; T_2 - T_1 = 9 \text{ and } T_3 - T_2 = 21$  $\therefore T_5 = 3 + 9 + 21 + 33 + 45 = 111$ OR/OF $2a = 12$ $a = 6$ $3(6) + b = 9$ $b = -9$ $6 - 9 + c = 3$ $T_5 = 6(5)^2 - 9(5) + 6 = 111$	$\checkmark$ constant second diff = 12 $\checkmark$ first differences : 33 and 45 (2) OR/OF $\checkmark$ constant second diff = 12 $\checkmark$ substitute 5 (2)

2.2.2	$2a = 12$ $a = 6$ $3(6) + b = 9$ or $5 \times 6 + b = 21$ $b = -9$ $6 - 9 + c = 3$ $c = 6$ $T_n = 6n^2 - 9n + 6$	$\checkmark 2a = 12$ $\checkmark 3(6) + b = 9 / 5 \times 6 + b = 21$ $\checkmark 6 - 9 + c = 3$ (3)
2.2.3	$T'_n = 12n - 9 > 0$ $n > \frac{3}{4}$ $\therefore T_n$ is increasing for $n \in N$ OR/OF $n = -\frac{b}{2a} = -\frac{-9}{2(6)}$ $n = \frac{3}{4}$ $\therefore$ min at $n = 1$ for $n \in N$ $\therefore T_n$ is increasing for $n \in N$	$\checkmark T'_n = 12n - 9$ $\checkmark n > \frac{3}{4}$ $\checkmark$ increasing for $n \in N$ (3) OR/OF $\checkmark n = -\frac{b}{2a} = \frac{9}{2(6)}$ $\checkmark n = \frac{3}{4}$ $\checkmark$ increasing for $n \in N$ (3)
		[16]

QUESTION 3/VRAAG 3

3.1.1	$T_n = ar^{n-1}$ $T_n = 3(2)^{n-1}$	$\checkmark T_n = 3(2)^{n-1}$ (1)
3.1.2	$\sum_{p=1}^k \frac{3}{2} \cdot 2^p = 98\,301$ $\sum_{p=1}^k \frac{3}{2} \cdot 2^p = 3 + 6 + 12 + \dots$ $n = k$ $\frac{3[(2)^k - 1]}{2 - 1} = 98\,301$ $(2)^k = 32\,768$ $2^k = 2^{15}$ OR/OF $k = \log_2 32\,768$ $\therefore k = 15$	$\checkmark$ expansion $\checkmark n = k$ $\checkmark$ substitution into correct formula $\checkmark k = 15$ (4)
3.2	$S_{22} = \frac{22}{2} [2a + 21(3)]$ $S_{22} = 22a + 693$ $S_{\infty} = \frac{a}{1 - \frac{1}{3}}$ $= \frac{3a}{2}$ $\therefore 22a + 693 = \frac{3a}{2} + 734$ $44a + 1386 = 3a + 1468$ $41a = 82$ $a = 2$	$\checkmark$ substitution into S_n $\checkmark S_{22} = 22a + 693$ $\checkmark$ substitution into S_{∞} $\checkmark S_{22} = S_{\infty} + 734$ $\checkmark$ answer (5)
		[10]

QUESTION 5/VRAAG 5

5.1	(1 ; 8)	✓ $x = 1$ ✓ $y = 8$ (2)
5.2	$y = -\frac{1}{2}(0-1)^2 + 8$ $= 7\frac{1}{2}$ $C\left(0; \frac{15}{2}\right)$	✓ $x = 0$ ✓ answer (2)
5.3	$8 = \frac{d}{1}$ $\therefore d = 8$	✓ substitution (1 ; 8) (1)
5.4	$y \in R; y \neq 0$	✓ $y \neq 0$ (1)
5.5	$-3 \leq x < 0$ or $x \geq 5$ OR/OF $x \in [-3; 0) \cup [5; \infty)$	✓✓ $-3 \leq x < 0$ ✓ $x \geq 5$ (3)
5.6	$-2x + k = \frac{8}{x}$ $-2x^2 + kx - 8 = 0$ $\Delta = (k)^2 - 4(-2)(-8)$ $k^2 - 64 < 0$ $CV: k = 8 ; k = -8$ $\therefore -8 < k < 8 \quad \text{or/of} \quad k \in (-8; 8)$ OR/OF $g'(x) = h'(x)$ $-\frac{8}{x^2} = -2$ $-8 = -2x^2$ $x = \pm 2$ $y = \pm 4 \quad \therefore B(2; 4) \text{ and } A(-2; -4)$ For tangents: $h(x) = -2x + k \quad \text{or} \quad h(x) = -2x + k$ $4 = -2(2) + k \quad \quad -4 = -2(-2) + k$ $k = 8 \quad \quad \quad k = -8$ $\therefore -8 < k < 8 \quad \text{or/of} \quad k \in (-8; 8)$	$-2x + k = \frac{8}{x}$ ✓ standard form ✓ substitution into Δ ✓ $\Delta < 0$ or $\Delta = 0$ ✓ inequality (5) OR/OF $-\frac{8}{x^2} = -2$ ✓ x-values ✓ y-values ✓ inequality (5)

QUESTION/VRAAG 5

5.1	$-2x^2 + 4x + 16 = 0$ $x^2 - 2x - 8 = 0$ $(x-4)(x+2) = 0$ $x = 4$ or $x = -2$ $\therefore A(-2;0)$ and $B(4;0)$	$\checkmark$ factors $\checkmark x = -2$ $\checkmark x = 4$ (3)
5.2	$f(x) = -2x^2 + 4x + 16$ $-\frac{b}{2a} = -\frac{-4}{-2(2)} = 1$ $f(1) = -2(1)^2 + 4(1) + 16 = 18$ $\therefore C(1;18)$ OR/OF $f(x) = -2x^2 + 4x + 16$ $f'(x) = -4x + 4$ $-4x + 4 = 0$ $x = 1$ $f(1) = -2(1)^2 + 4(1) + 16 = 18$ $\therefore C(1;18)$	$\checkmark 1$ $\checkmark 18$ (2) OR/OF $\checkmark 1$ $\checkmark 18$ (2)
5.3	$y \leq 18$ OR/OF $y \in (-\infty; 18]$	$\checkmark y \leq 18$ (1) OR/OF $\checkmark y \in (-\infty; 18]$ (1)
5.4	TP (1 ; 18) for f TP (2 ; 15) for h $\therefore p = -1$ $q = -3$	$\checkmark$ TP for h at (2 ; 15) $\checkmark p = -1$ $\checkmark q = -3$ (3)
5.5	$y = 2x + 4$ $x = 2y + 4$ $\therefore y = \frac{1}{2}x - 2$	$\checkmark$ swop x and y $\checkmark y = \frac{1}{2}x - 2$ (2)
5.6	$g(x) = 0$ or $g^{-1}(x) = 0$ $x = 4$ or $x = -2$ (product 0 at x -intercepts)	$\checkmark x = 4$ $\checkmark x = -2$ (2)

5.7	$-2x^2 + 4x + 16 + k = 2x + 4$ $-2x^2 + 2x + 12 + k = 0$ $b^2 - 4ac < 0$ $(2)^2 - 4(-2)(12 + k) < 0$ $4 + 8(12 + k) < 0$ $100 + 8k < 0$ $k < -12,5$ OR/OF $g'(x) = 2$ $f'(x) = -4x + 4 = 2$ $x = \frac{1}{2}$ $f\left(\frac{1}{2}\right) = 17,5$ $g\left(\frac{1}{2}\right) = 5$ $\therefore k < -12,5$	✓ equating ✓ standard form ✓ $b^2 - 4ac < 0$ ✓ substitution ✓ answer (5) OR/OF ✓ $g'(x) = 2$ ✓ $f'(x) = -4x + 4$ ✓ $f\left(\frac{1}{2}\right) = 17,5$ ✓ $g\left(\frac{1}{2}\right) = 5$ ✓ answer (5)
		[18]

QUESTION/VRAAG 6

6.1.1	$y = 3^x$ $x = 3^y$ $y = \log_3 x$	✓ swop x and y ✓ equation (2)
6.1.2	$h(x) = 3^{x-4} + 2$ Transformation: 4 units left, 2 units down $P'(2;9)$	✓ $x = 2$ (A) ✓ $y = 9$ (A) (2)
6.2	$f(x) = 2^{x+p} + q$ $q = -16$ $16 = 2^{p+3} - 16$ $2^{p+3} = 32$ $2^{p+3} = 2^5$ $\therefore p + 3 = 5$ $p = 2$	✓ $q = -16$ ✓ substitute (3 ; 16) ✓ $2^{p+3} = 2^5$ or $p + 3 = \log_2 32$ ✓ $p = 2$ (4)
		[8]

QUESTION/VRAAG 4

4.1	M(3 ; 4)	✓ x -value ✓ y- value (2)
4.2	$f(x) = \frac{4}{x-3} + 4$ $y = \frac{4}{0-3} + 4 = \frac{8}{3}$ $\therefore D\left(0; \frac{8}{3}\right)$	✓ x = 0 ✓ y-value (2)
4.3	M(3 ; 4) $y = x + t$ OR/OF $y = (x + p) + q$ $4 = 3 + t$ $y = x - 3 + 4$ $t = 1$ $y = x + 1$ $\therefore t = 1$	✓ substituting M(3 ; 4) ✓ value of t (2)
4.4	$\frac{4}{x-3} + 4 = 0$ $-4(x-3) = 4$ $x-3 = -1$ $x = 2$ C(2 ; 0) $\therefore 2 \leq x < 3$	✓ y = 0 ✓ x = 2 ✓✓ answer (4)
4.5	$\frac{4}{x-3} + 4 = x + 1$ $\frac{4}{x-3} = x - 3$ $4 = (x-3)^2$ $\pm 2 = x - 3$ $\therefore x = 5 \quad \text{or} \quad x \neq 1$ $\therefore A(5 ; 6)$ OR/OF Point closest to the origin in $y = \frac{a}{x}$ is $(\sqrt{a}; \sqrt{a})$ By translation: A($\sqrt{a} + 3$; $\sqrt{a} + 4$) A(5 ; 6)	✓equating ✓✓ A OR/OF ✓translation ✓✓ A (3)
4.6	$h(x) = \frac{-4}{x+3} + 4 = \frac{4}{-x-3} + 4$ $\therefore$ Reflection in y - axis. A'(-5;6) AA' = 10	✓ coordinate ✓ distance (2)
		[15]

QUESTION/VRAAG 8

8.1	$f(x) = 3x^2$ $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ $f'(x) = \lim_{h \rightarrow 0} \frac{3(x+h)^2 - 3x^2}{h}$ $f'(x) = \lim_{h \rightarrow 0} \frac{3x^2 + 6xh + 3h^2 - 3x^2}{h}$ $= \lim_{h \rightarrow 0} \frac{6xh + 3h^2}{h}$ $= \lim_{h \rightarrow 0} \frac{h(6x + 3h)}{h}$ $= 6x$	✓ substitution ✓ expansion ✓ simplification ✓ $\lim_{h \rightarrow 0} \frac{h(6x + 3h)}{h}$ ✓ $6x$ (5)
8.2.1	$f(x) = x^2 - 3 + 9x^{-2}$ $f'(x) = 2x - 18x^{-3}$	✓ $9x^{-2}$ ✓ $2x$ ✓ $-18x^{-3}$ (3)

QUESTION/VRAAG 4

4.1	M(3 ; 4)	✓ x –value ✓ y- value (2)
4.2	$f(x) = \frac{4}{x-3} + 4$ $y = \frac{4}{0-3} + 4 = \frac{8}{3}$ $\therefore D\left(0; \frac{8}{3}\right)$	✓ x = 0 ✓ y-value (2)
4.3	M(3 ; 4) $y = x + t$ $4 = 3 + t$ $t = 1$	OR/OF $y = (x + p) + q$ $y = x - 3 + 4$ $y = x + 1$ $\therefore t = 1$ ✓ substituting M(3 ; 4) ✓ value of t (2)
4.4	$\frac{4}{x-3} + 4 = 0$ $-4(x-3) = 4$ $x-3 = -1$ $x = 2$ $C(2 ; 0)$ $\therefore 2 \leq x < 3$	✓ y = 0 ✓ x = 2 ✓✓ answer (4)
4.5	$\frac{4}{x-3} + 4 = x + 1$ $\frac{4}{x-3} = x - 3$ $4 = (x-3)^2$ $\pm 2 = x - 3$ $\therefore x = 5 \quad \text{or} \quad x = 1$ $\therefore A(5 ; 6)$ OR/OF Point closest to the origin in $y = \frac{a}{x}$ is $(\sqrt{a}; \sqrt{a})$ By translation: $A(\sqrt{a} + 3; \sqrt{a} + 4)$ $A(5 ; 6)$	✓equating ✓✓ A OR/OF ✓translation ✓✓ A (3)
4.6	$h(x) = \frac{-4}{x+3} + 4 = \frac{4}{-x-3} + 4$ $\therefore \text{Reflection in } y - \text{axis.}$ $A'(-5; 6)$ $AA' = 10$	✓ coordinate ✓ distance (2)
		[15]

8.2.2	$g(x) = (\sqrt{x}+3)(\sqrt{x}-1)$ $g(x) = x + 2x^{\frac{1}{2}} - 3$ $g'(x) = 1 + x^{-\frac{1}{2}}$	$\checkmark x \quad \checkmark 2x^{\frac{1}{2}}$ $\checkmark 1 \quad \checkmark x^{-\frac{1}{2}}$ (4)
		[12]

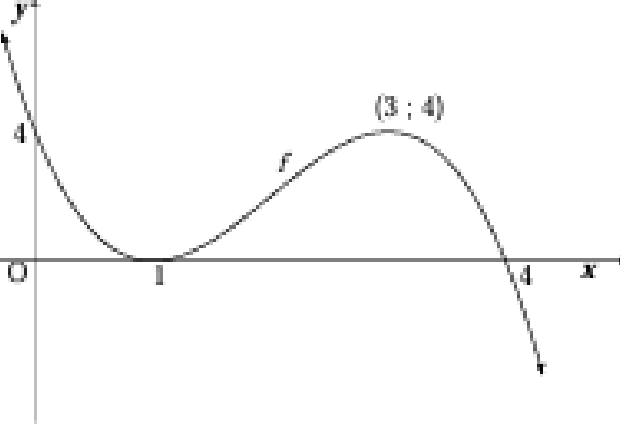
QUESTION/VRAAG 9

9.1	$f'(x) = 6x^2 + 6x - 12$ $6x^2 + 6x - 12 = 0$ $x^2 + x - 2 = 0$ $(x+2)(x-1) = 0$ $x = -2 \quad \text{or} \quad x = 1$ $y = 20 \quad \text{or} \quad y = -7$ $\therefore A(-2; 20) \text{ and } B(1; -7)$	$\checkmark 6x^2 + 6x - 12$ $\checkmark = 0$ $\checkmark \text{factors}$ $\checkmark x\text{-values}$ $\checkmark y\text{-values}$ (5)
9.2	$f''(x) = 12x + 6$ $12x + 6 > 0$ $12x > -6$ $x > -\frac{1}{2}$ OR/OF $x = \frac{-2+1}{2} = -\frac{1}{2}$ $\therefore x > -\frac{1}{2}$	$\checkmark 12x + 6$ $\checkmark f''(x) > 0$ $\checkmark x > -\frac{1}{2}$ (3) OR/OF $\checkmark x = -\frac{1}{2}$ $\checkmark \checkmark x > -\frac{1}{2}$ (3)
9.3	$f'(2) = 24$ Equation of the tangent: $y - 4 = 24(x - 2)$ $y = 24x - 44$	$\checkmark f'(2)$ $\checkmark 24$ $\checkmark \text{equation}$ (3)
		[11]

QUESTION 7/VRAAG 7

7.1	$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ $f'(x) = \lim_{h \rightarrow 0} \frac{-4(x+h)^2 - (-4x^2)}{h}$ $f'(x) = \lim_{h \rightarrow 0} \frac{-4x^2 - 8xh - 4h^2 + 4x^2}{h}$ $f'(x) = \lim_{h \rightarrow 0} \frac{-8xh - 4h^2}{h}$ $f'(x) = \lim_{h \rightarrow 0} \frac{h(-8x - 4h)}{h}$ $f'(x) = \lim_{h \rightarrow 0} (-8x - 4h)$ $f'(x) = -8x$ OR/OF $f(x+h) = -4(x+h)^2 = -4x^2 - 8xh - 4h^2$ $f(x+h) - f(x) = -4x^2 - 8xh - 4h^2 - (-4x^2)$ $= -8xh - 4h^2$ $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ $f'(x) = \lim_{h \rightarrow 0} \frac{-8xh - 4h^2}{h}$ $f'(x) = \lim_{h \rightarrow 0} \frac{h(-8x - 4h)}{h}$ $f'(x) = \lim_{h \rightarrow 0} (-8x - 4h)$ $f'(x) = -8x$	✓ substitution into correct formula ✓ $f(x+h) = -4x^2 - 8xh - 4h^2$ ✓ simplification ✓ common factor ✓ answer (5) OR/OF ✓ $f(x+h) = -4x^2 - 8xh - 4h^2$ ✓ simplification ✓ substitution into correct formula ✓ common factor ✓ answer (5)
7.2.1	$f(x) = 2x^3 - 3x$ $f'(x) = 6x^2 - 3$	✓ $6x^2$ ✓ -3 (2)
7.2.2	$D_x \left[7\sqrt[3]{x^2} + 2x^{-5} \right]$ $D_x \left[7x^{\frac{2}{3}} + 2x^{-5} \right]$ $= \frac{14}{3} x^{-\frac{1}{3}} - 10x^{-6}$	✓ $x^{\frac{2}{3}}$ ✓ derivative with rational exp ✓ $-10x^{-6}$ (3)
7.3	$-6x^2 + 8 > 0$ $x^2 < \frac{8}{6}$ CV's: $x = -\frac{2}{\sqrt{3}}$ or $x = \frac{2}{\sqrt{3}}$ Positive for: $-\frac{2}{\sqrt{3}} < x < \frac{2}{\sqrt{3}}$	✓ CV's: $x = \pm \frac{2}{\sqrt{3}}$ ✓ ✓ answer (3)
		[13]

QUESTION 8/ VRAAG 8

8.1	$f'(x) = -3x^2 + 12x - 9$ $-3x^2 + 12x - 9 = 0$ $x^2 - 4x + 3 = 0$ $(x-3)(x-1) = 0$ $\therefore x = 3$ or $x = 1$ $f(3) = -(3)^3 + 6(3)^2 - 9(3) + 4 = 4$ $f(1) = -(1)^3 + 6(1)^2 - 9(1) + 4 = 0$ $\therefore$ turning points are: (3 ; 4) and (1 ; 0)	✓ $f'(x) = -3x^2 + 12x - 9$ ✓ $f'(x) = 0$ ✓ both x -values ✓ both y -values (4)
8.2		✓ y -intercept ✓ both x -intercepts ✓ both turning points ✓ shape (4)
8.3	$0 < k < 4$ or/af $k \in (0 ; 4)$	✓✓ k between y -values of turning points (2)
8.4	$f''(x) = -6x + 12 = 0$ $x = 2$ Max at (2 ; 2) $f'(2) = 3$ $\therefore y - 2 = 3(x - 2)$ or $2 = 3(2) + c$ $g(x) = 3x - 4$ $g(x) = 3x - 4$ OR/OF Point of inflection: $x = \frac{3+1}{2}$ $x = 2$ Max at (2 ; 2) $f'(2) = 3$ $\therefore y - 2 = 3(x - 2)$ or $2 = 3(2) + c$ $g(x) = 3x - 4$ $g(x) = 3x - 4$	✓ $f''(x) = -6x + 12$ ✓ $f''(x) = 0$ ✓ x -value ✓ y -value ✓ gradient at x -value ✓ equation of tangent (6) OR/OF ✓✓ $\frac{3+1}{2}$ ✓ x -value ✓ y -value ✓ gradient at x -value ✓ equation of tangent (6)
8.5	$\tan \theta = 3$ $\therefore \theta = 71,57^\circ$	✓ gradient of g ✓ answer (2)
		[18]